

The x and y intercepts of a line are the points at which the line crosses the x and y axes, respectively. These points are of the form $(a,0)$ and $(0,b)$, but they are usually represented simply by a and b , since the O 's are understood by their position on the axes. It might be noted that lines parallel to the x-axis have no x intercept and those parallel to the y-axis have no y intercept.

Slope-Intercept Form of a line with slope m and y intercept b or $(0,b)$ has the equation:

$$y = mx + b$$

Intercept Form of a line with nonzero intercepts a and b or $(a,0)$ and $(0,b)$ has the equation:

$$\frac{x}{a} + \frac{y}{b} = 1$$

General Form of a line where integers A and B are not both zero has the equation: $Ax + By + C = 0$

Standard Form of a line where integers A and B are not both zero has the equation: $Ax + By = C$

Guided Practice

2/102

$m = -1, b = 3$

the slope and y intercept implies using the slope-intercept form

$$y = mx + b$$

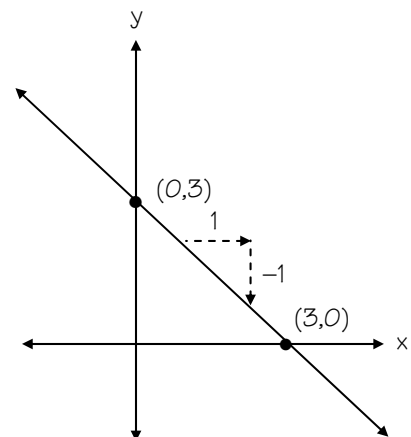
$$y = (-1)x + (3)$$

$$y = -x + 3 \quad \text{slope-intercept form}$$

$$x + y = 3 \quad \text{standard form}$$

$$x + y - 3 = 0 \quad \text{general form}$$

$$\frac{x}{3} + \frac{y}{3} = 1 \quad \text{intercept form}$$



Guided Practice

8/102

$m = 6, a = 3$

the slope and x intercept implies using the point – slope form

$m = 6, (3, 0)$

$y = m(x - x_1) + y_1$

$y = 6(x - 3) + 0$

$y = 6x - 18 + 0$

$y = 6x - 18$

slope – intercept form

$18 = 6x - y$

$6x - y = 18$

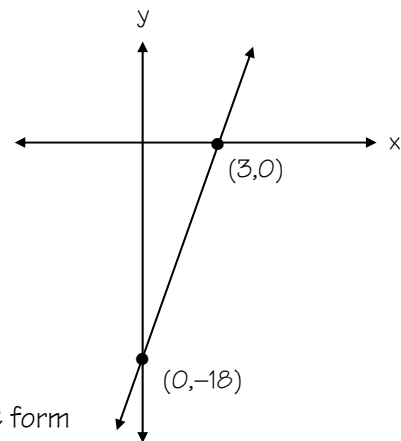
standard form

$6x - y - 18 = 0$

general form

$\frac{x}{3} + \frac{y}{-18} = 1$

intercept form



10/102

no m , $a = 2$

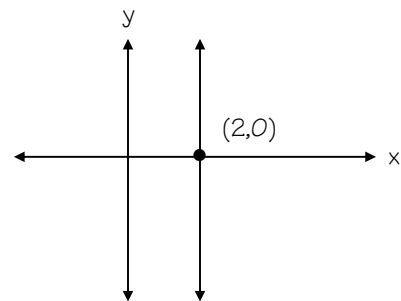
no slope and x intercept implies vertical line $x = a$

$m = \text{DNE}, (2, 0)$

$x = 2$

$x - 2 = 0$

general form



18/102

$a = b = 0$, through $(-2, -3)$

two points implies using the two – point form

 $a = 0$ and $b = 0$ implies origin $(0, 0)$ intercepts

$y = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1) + y_1$

$y = \frac{-3 - 0}{-2 - 0}(x - 0) + 0$

$y = \frac{3}{2}x - 0$

slope – intercept form

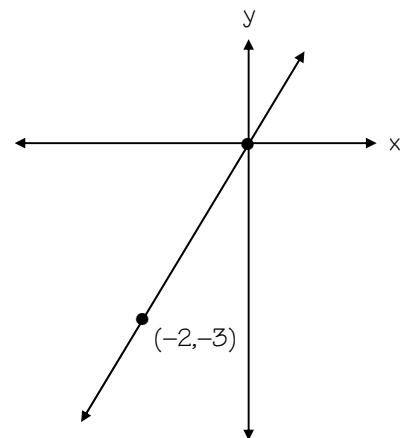
$2y = 3x$

$3x - 2y = 0$

standard form

$3x - 2y + 0 = 0$

general form



Guided Practice**22/102**perpendicular to $x + 2y - 5 = 0$ and containing the point $(4,1)$

$$x + 2y - 5 = 0$$

$$2y = -x + 5$$

$$y = \frac{-x + 5}{2}$$

$$y = -\frac{1}{2}x + \frac{5}{2}$$

$$m = -\frac{1}{2}$$

$$m_{\perp} = 2 \text{ and } (4,1)$$

$$y = m(x - x_1) + y_1$$

$$y = 2(x - 4) + 1$$

$$y = 2x - 8 + 1$$

$$y = 2x - 7$$

$$y = 2x - 7$$

slope-intercept form

$$2x - 7 = y$$

$$2x - y = 7$$

standard form

$$2x - y - 7 = 0$$

general form

24/102 $a = 3b \neq 0$, through $(5, -4)$ a and $b \neq 0$ implies using the intercept form

substitute

$$x = 5, y = -4, a = 3b$$

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{5}{3b} + \frac{-4}{b} = 1$$

$$3b \left[\frac{5}{3b} + \frac{-4}{b} \right] = 3b[1]$$

$$5 + 3(-4) = 3b$$

$$5 - 12 = 3b$$

$$-7 = 3b$$

$$b = -\frac{7}{3}$$

$$y\text{-intercept} = \left(0, -\frac{7}{3}\right)$$

$$a = 3b$$

$$a = 3\left(-\frac{7}{3}\right)$$

$$a = -7$$

$$x\text{-intercept} = (-7, 0)$$

substitute

$$a = -7, b = -\frac{7}{3}$$

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{-7} + \frac{y}{-\frac{7}{3}} = 1$$

$$\frac{x}{-7} + \frac{y}{-\frac{7}{3}} = 1$$

$$\frac{x}{-7} + \left(\frac{y}{1}\right)\left(-\frac{3}{7}\right) = 1$$

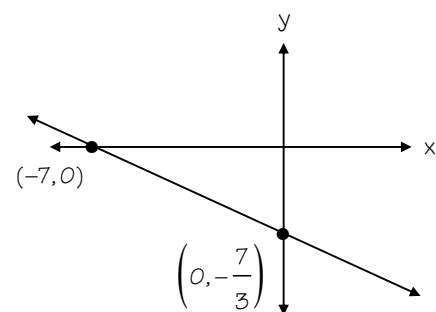
$$\frac{x}{-7} - \frac{3y}{7} = 1$$

$$-7 \left[-\frac{x}{7} - \frac{3y}{7} \right] = -7[1]$$

$$x + 3y = -7$$

$$x + 3y + 7 = 0$$

general form



$$\frac{x}{-7} + \frac{y}{-\frac{7}{3}} = 1$$

intercept form